

Chapter 4 Function Minimization Algorithms (III)

Prime Implicant Tables for Multiple Output Problems (1/4)

- Consider finding the minimum output of the set of functions

$$f(a,b,c) = \sum m(2,3,7)$$

$$g(a,b,c) = \sum m(4,3,7)$$

- Essential prime implicants are found as before. An X is placed in the column of a function for which the term is an implicant

Table 4.9 A multiple output prime implicant table.

	S		<i>f</i>			<i>g</i>		
			✓ 2	✓ 3	7	✓ 4	✓ 5	7
1 1 1	4	<i>A</i>			X			X
0 1 -*	3	<i>B</i>	X	X				
1 0 -*	3	<i>C</i>				X	X	
- 1 1	3	<i>D</i>		X	X			
1 - 1	3	<i>E</i>					X	X

Prime Implicant Tables for Multiple Output Problems (2/4)

- The table is then reduced as in Table 4.10

Table 4.10 A reduced prime implicant table.

			f	g
			7	7
1 1 1	4	A	X	X
- 1 1	3	D	X	
1 - 1	3	E		X

- It is clear that we can use term A to cover both functions, rather than two separate terms, even though A costs 4 and the others cost 3

Prime Implicant Tables for Multiple Output Problems (3/4)

- The solution is thus

$$f = a'b + abc$$

$$g = ab' + abc$$

- **Example 4.12.** Consider finding the minimum output of the functions

$$f(a, b, c, d) = \Sigma m(2, 3, 4, 6, 9, 11, 12) + \Sigma d(0, 1, 14, 15)$$

$$g(a, b, c, d) = \Sigma m(2, 6, 10, 11, 12) + \Sigma d(0, 1, 14, 15)$$

- Don't Cares will not be considered again because all the prime implicants (including Don't Cares) are found by Q-M method or Iterated Consensus method. They are listed below

Prime Implicant Tables for Multiple Output Problems (4/4)

			<i>f</i>							<i>g</i>				
			2	3 [✓]	4	6	9 [✓]	11 [✓]	12	2	6	10	11	12 [✓]
0 0 0 -	A	4												
0 0 - 0	B	4	X							X				
0 - 1 0	C	4	X			X				X	X			
- 1 1 0	D	4				X					X			
1 - 1 1	E	4						X					X	
1 1 1 -	F	4												
1 1 - 0*	G	4							X					X
- 1 - 0	H	3			X	X			X					
0 - - 0	J	3	X		X	X								
0 0 - -	K	3	X	X										
- 0 - 1*	L	3		X			X	X						
- - 1 0	M	3								X	X	X		
1 - 1 -	N	3										X	X	

For sharing

For *f*

For *g*

Not shared with *g*